

Supersymmetric extensions of the Standard Model

(Lecture 3 of 4)

Heather Logan
Carleton University

Hadron Collider Physics Summer School
Fermilab, August 2010

Outline

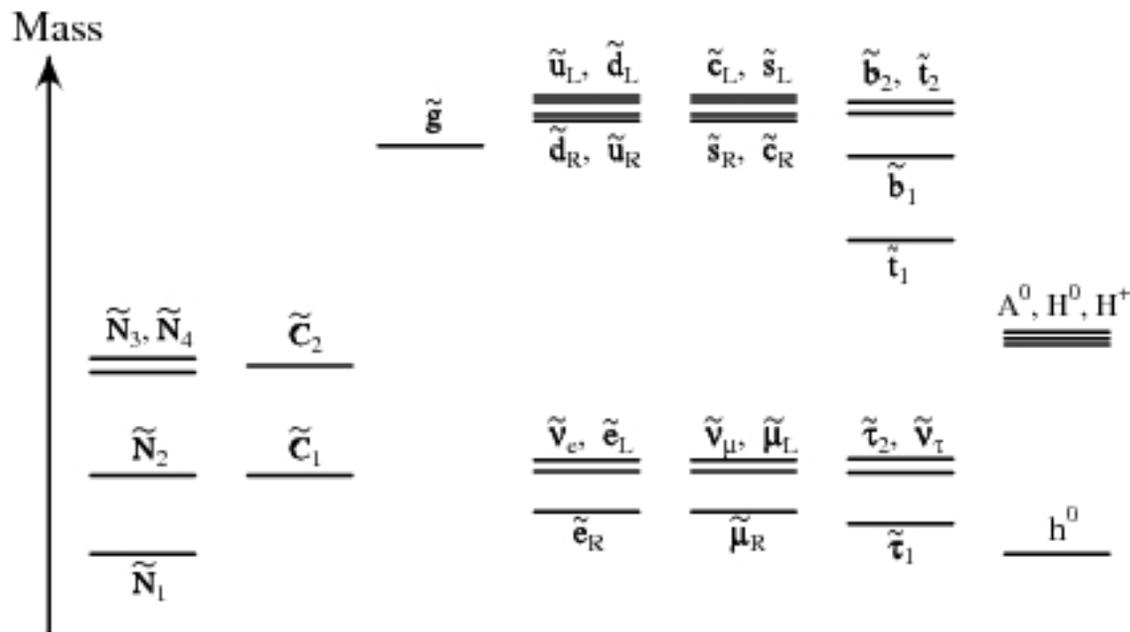
Lecture 1: Introducing SUSY

Lecture 2: SUSY Higgs sectors

Lecture 3: Superpartner spectra and detection

Lecture 4: Measuring spins, couplings, and masses

In my first lecture I showed a schematic sample SUSY spectrum (which may or may not have anything to do with reality):



Some features:

- \tilde{N}_1 is the LSP
- \tilde{t}_1 and \tilde{b}_1 are the lightest squarks
- $\tilde{\tau}_1$ is the lightest charged slepton
- Colored particles are heavier than uncolored particles

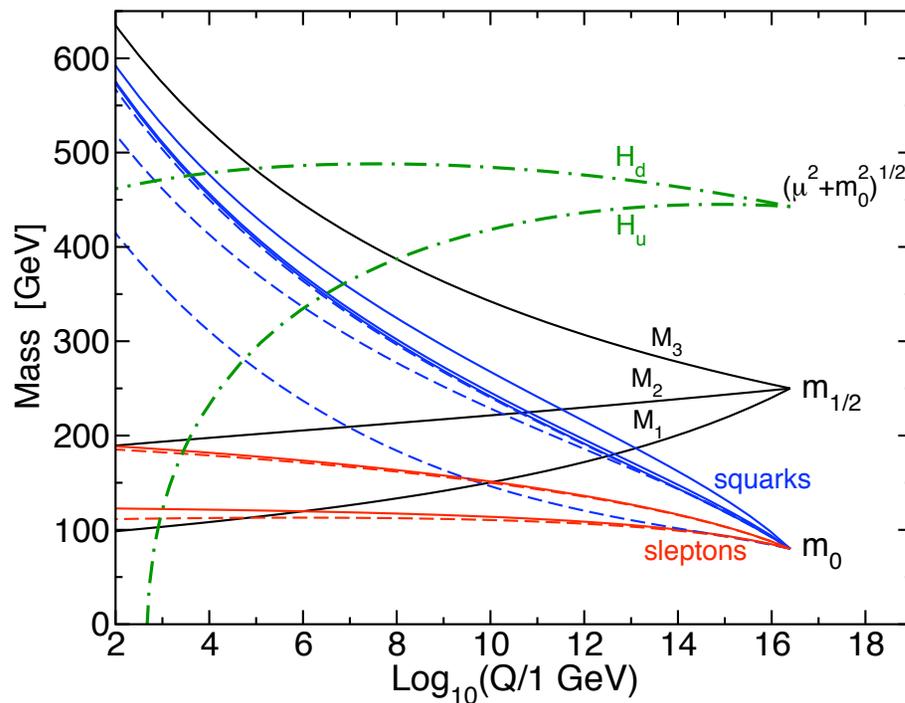
from Martin, hep-ph/9709356

Where do these features come from?

SUSY particle masses are (presumably) set at a high scale by some SUSY-breaking mechanism.

Masses run down by renormalization group equations.

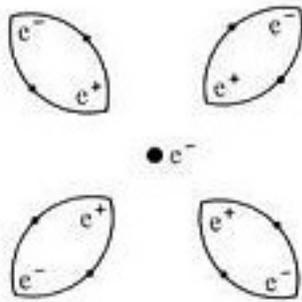
E.g., “Constrained MSSM” (CMSSM, a.k.a. mSUGRA):



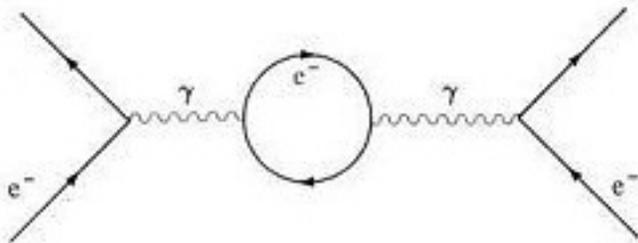
from Martin, [hep-ph/9709356](https://arxiv.org/abs/hep-ph/9709356)

To do phenomenology, we need to know what the SUSY breaking terms are at the electroweak scale.

These are different from the high-scale SUSY breaking terms because of [vacuum polarization](#).



Charge measured at large distance (low energy) is different from charge measured at short distance (high energy) due to screening by virtual particles.



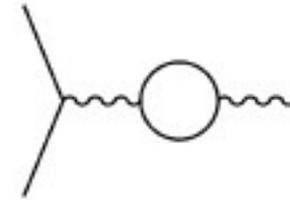
[figure stolen from [universe-review.ca](#)]

Same idea applicable to other couplings, masses, etc.

Coupling dependence on scale is encoded in [renormalization group equations](#).

Gauge couplings: Running is given by the **beta functions** b_a .

$$\frac{d}{dt}\alpha_a^{-1} = -\frac{b_a}{2\pi} \quad (a = 1, 2, 3)$$



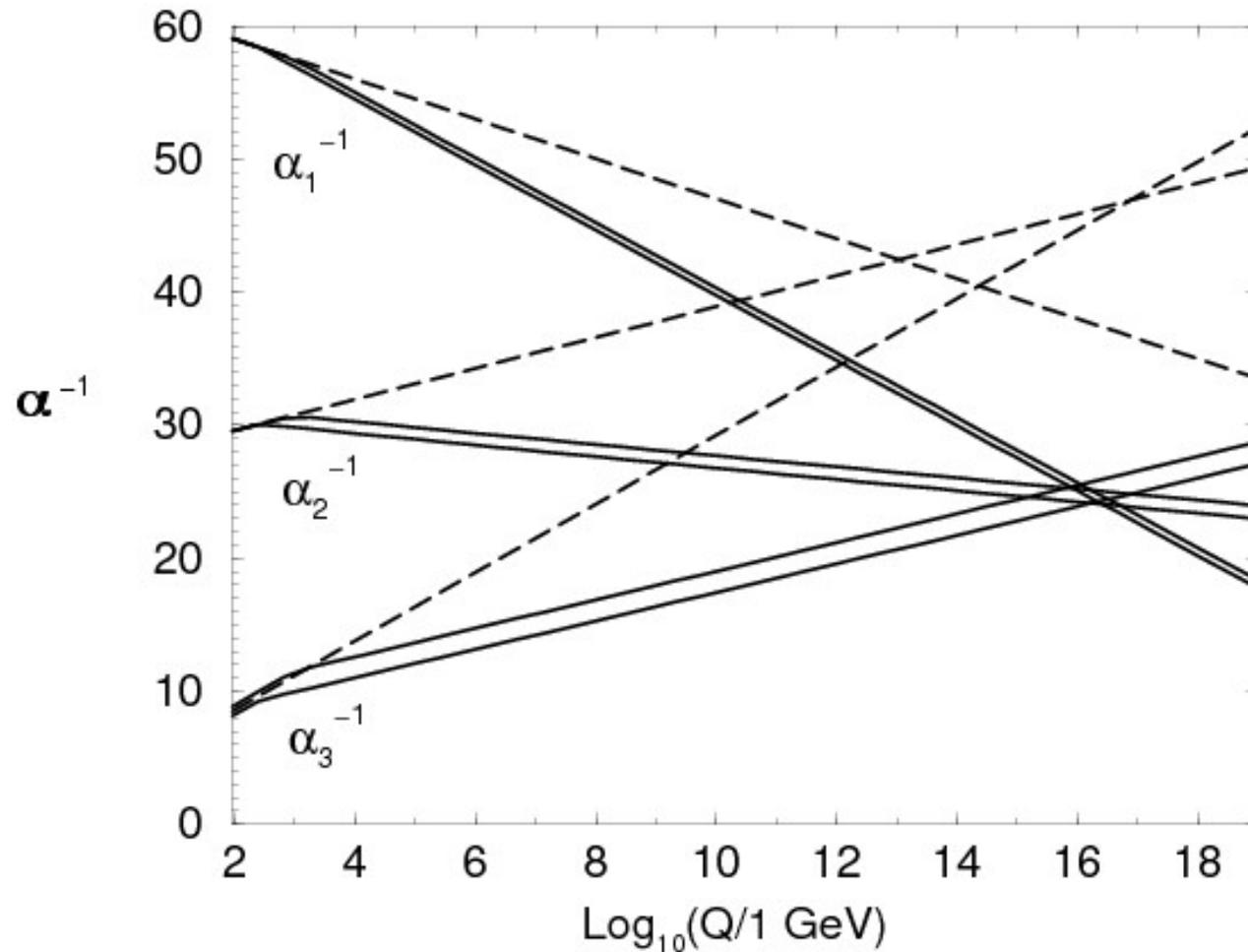
- the energy scale dependence is encoded by $t \equiv \ln(Q/Q_0)$
 Q is the “current” scale; Q_0 is the starting scale
- $a = 1, 2, 3$ refers to $U(1)_Y$, $SU(2)_L$, and $SU(3)_c$ gauge couplings
- The beta functions b_a are what you get when you calculate all the loop diagrams:

$$b_a^{\text{SM}} = \left(\frac{41}{10}, -\frac{19}{6}, -7 \right) \quad b_a^{\text{MSSM}} = \left(\frac{33}{5}, 1, -3 \right)$$

These depend on the number of particles and their gauge charges.

Gauge couplings:

figure from Martin, hep-ph/9709356



Dashed lines: SM

Solid lines: MSSM

(Bands are the uncertainties in the low-energy values.)

Here's another glory of SUSY: gauge coupling unification!

Gaugino mass parameters:

Running determined by same b_a as gauge couplings:

$$\frac{d}{dt}M_a = \frac{1}{8\pi^2}b_a g_a^2 M_a \quad b_a^{\text{MSSM}} = \left(\frac{33}{5}, 1, -3\right)$$

Ratios M_a/g_a^2 are **scale independent** up to small 2-loop effects.

In mSUGRA (Constrained MSSM), the gaugino masses **unify**:

$$M_1(M_{\text{Pl}}) = M_2(M_{\text{Pl}}) = M_3(M_{\text{Pl}}) \equiv m_{1/2}$$

Gauge couplings also unify nearby, at $M_{\text{GUT}} \simeq 0.01M_{\text{Pl}}$, so

$$g_1^2(M_{\text{Pl}}) \approx g_2^2(M_{\text{Pl}}) \approx g_3^2(M_{\text{Pl}}) \approx g_{\text{GUT}}^2 \quad [g_1 = \sqrt{5/3}g': \text{GUT norm'n}]$$

Therefore in the CMSSM (and any model with gaugino mass unification near M_{Pl}),

$$\frac{M_1}{g_1^2} \simeq \frac{M_2}{g_2^2} \simeq \frac{M_3}{g_3^2} \simeq \frac{m_{1/2}}{g_{\text{GUT}}^2}$$

Low-scale gaugino mass parameters satisfy **unification relations**:

$$M_1 = \frac{g_1^2}{g_2^2} M_2 \simeq 0.5 M_2 \qquad M_3 = \frac{g_3^2}{g_2^2} M_2 \simeq 3.5 M_2$$

M_1 : bino mass parameter, controls mass of lightest neutralino in mSUGRA.

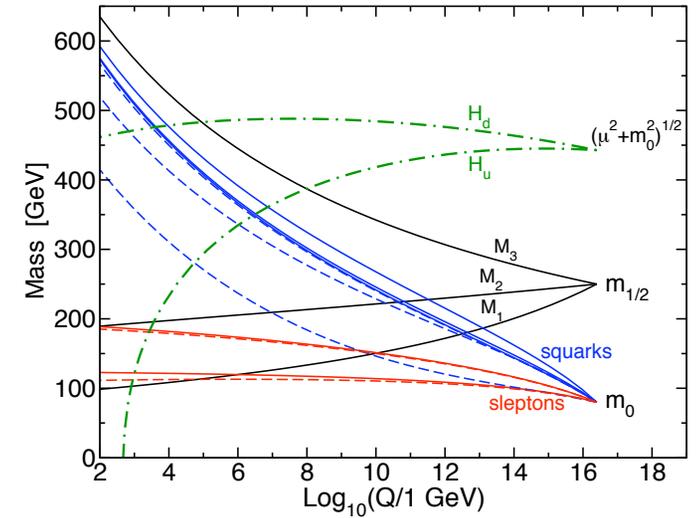
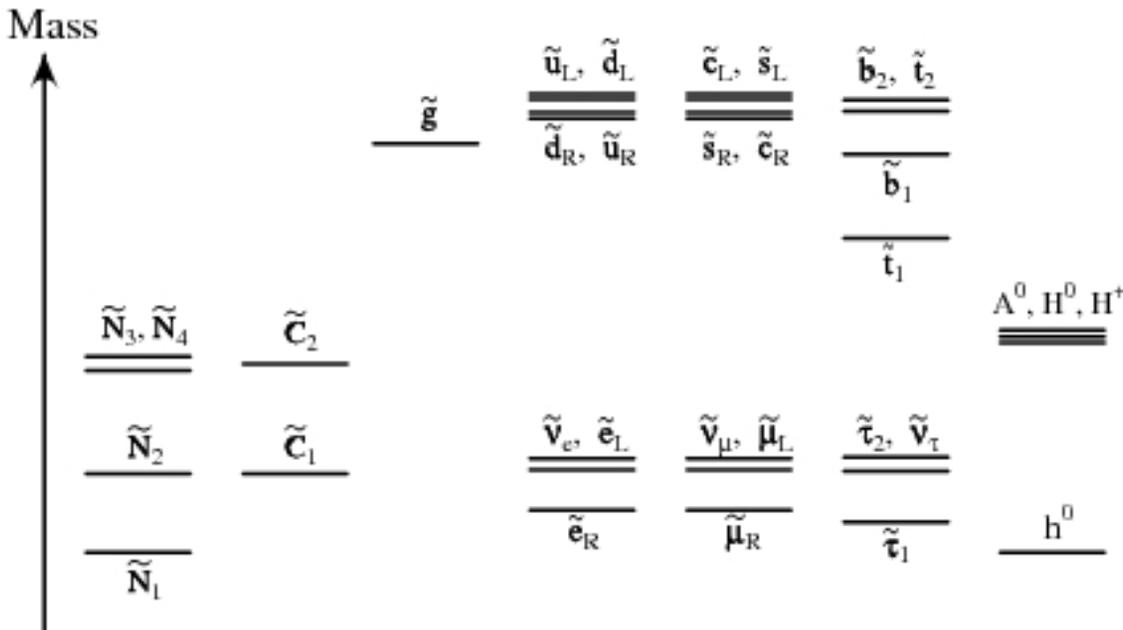
M_2 : wino mass parameter, controls mass of one chargino and one neutralino.

(Other chargino and two neutralinos controlled by Higgsino mass parameter μ)

M_3 : gluino mass parameter: this is the mass of the gluino.

This unification assumption underlies usually-quoted mass limits on lightest neutralino: really the limit is on M_2 from chargino searches at LEP and Tevatron.

These relations can be avoided in models in which the gaugino masses do not unify at the GUT scale; e.g. gauge mediated models.



from Martin, hep-ph/9709356

Gaugino mass unification:

$$M_1 = \frac{g_1^2}{g_2^2} M_2 \simeq 0.5 M_2$$

$$M_3 = \frac{g_3^2}{g_2^2} M_2 \simeq 3.5 M_2$$

$$M_{\tilde{N}_1} \simeq 0.5 M_{\tilde{N}_2, \tilde{C}_1}$$

$$M_{\tilde{g}} \simeq 3.5 M_{\tilde{N}_2, \tilde{C}_1}$$

These relations can be avoided in models in which the gaugino masses do not unify at the GUT scale; e.g. gauge mediated models.

Higgs sector mass parameters

recall $V_{\text{breaking}} \supset m_{H_1}^2 H_1^\dagger H_1 + m_{H_2}^2 H_2^\dagger H_2$

$$16\pi^2 \frac{d}{dt} m_{H_1}^2 = 3X_b + X_\tau - 6g_2^2 |M_2|^2 - \frac{6}{5}g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{H_2}^2 = 3X_t - 6g_2^2 |M_2|^2 - \frac{6}{5}g_1^2 |M_1|^2$$

X_t, X_b, X_τ are some convenient positive-definite parameter combinations,

$$X_t = 2|y_t|^2 (m_{H_u}^2 + m_{Q_3}^2 + m_{u_3}^2) + 2|a_t|^2$$

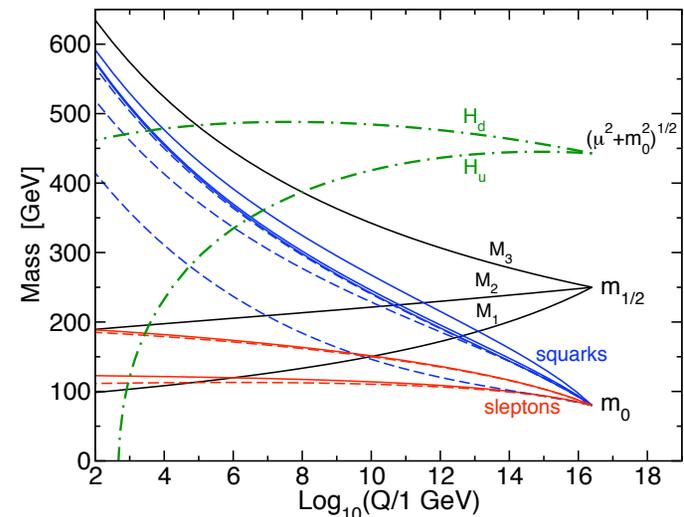
$$X_b = 2|y_b|^2 (m_{H_d}^2 + m_{Q_3}^2 + m_{d_3}^2) + 2|a_b|^2$$

$$X_\tau = 2|y_\tau|^2 (m_{H_d}^2 + m_{L_3}^2 + m_{e_3}^2) + 2|a_\tau|^2$$

$X_{t,b,\tau}$ decrease the Higgs masses as you evolve down from the GUT scale.

Can start with positive m_{H_u} and m_{H_d} at the GUT scale and have them run negative by the EW scale.

This is radiative electroweak symmetry breaking – usually caused by X_t because y_t is large.



from Martin, hep-ph/9709356

Squark and slepton mass parameters:

The RGEs for the 3rd generation are:

$$16\pi^2 \frac{d}{dt} m_{Q_3}^2 = X_t + X_b - \frac{32}{3} g_3^2 |M_3|^2 - 6g_2^2 |M_2|^2 - \frac{2}{15} g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{u_3}^2 = 2X_t - \frac{32}{3} g_3^2 |M_3|^2 - \frac{32}{15} g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{d_3}^2 = 2X_b - \frac{32}{3} g_3^2 |M_3|^2 - \frac{8}{15} g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{L_3}^2 = X_\tau - 6g_2^2 |M_2|^2 - \frac{3}{5} g_1^2 |M_1|^2$$

$$16\pi^2 \frac{d}{dt} m_{e_3}^2 = 2X_\tau - \frac{24}{5} g_1^2 |M_1|^2$$

RGEs for 1st and 2nd generations are the same but without the $X_{t,b,\tau}$ Yukawa contributions.

Large g_3^2 contribution runs squarks heavier than sleptons.

$X_{t,b,\tau}$ contributions run 3rd gen lighter than 1st & 2nd. [dashed lines]

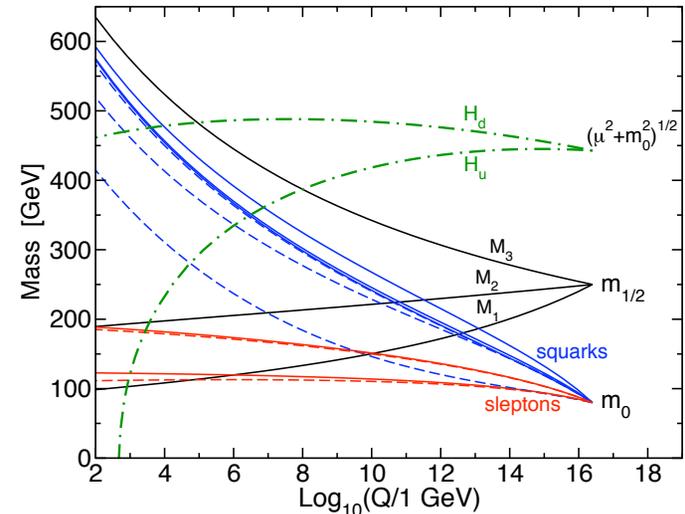
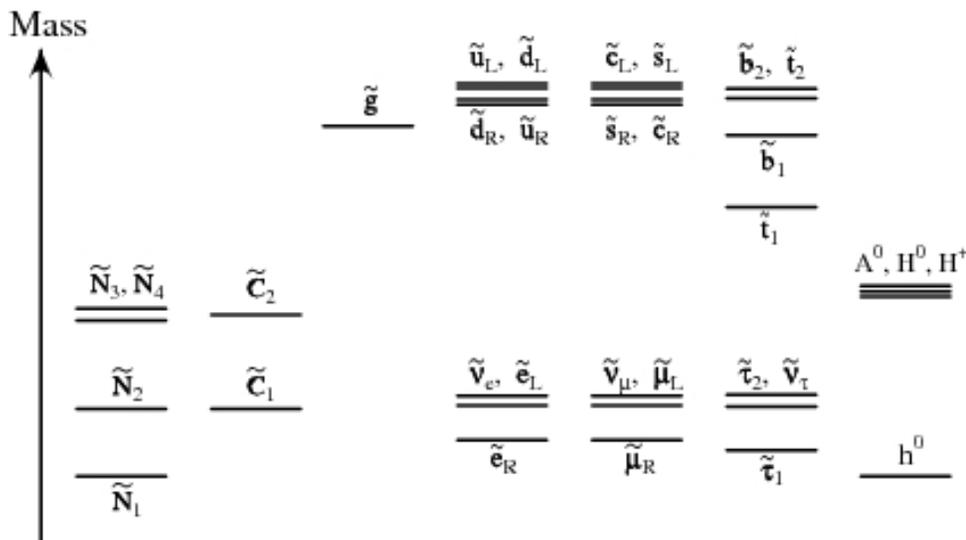


figure from Martin, hep-ph/9709356

What have we learned from the RGEs?

- Squarks run heavier than sleptons due to g_3^2 contribution.
 - Gluino runs heavier than weak gauginos due to strong g_3 .
- Expect colored sparticles to be heavier than uncolored sparticles.
[if their high-scale masses are not too different]

- Third generation runs lighter due to Yukawa contributions.
- Combined with $\tilde{f}_L - \tilde{f}_R$ mixing in 3rd gen, expect lightest squark, slepton to be 3rd-gen.



Collider complementarity

LHC: Produce heavy colored particles via QCD; lighter uncolored particles harder to see (lower rates).

ILC: Produce lighter uncolored particles via EW interactions; heavy colored particles beyond kinematic reach.

SUSY particles and collider phenomenology

The general features of SUSY phenomenology are controlled by:

R-parity conservation [introduced to avoid fast proton decay]

- Lightest R-odd particle (LSP) is stable
- Decay chains of R-odd (SUSY) particles must end in LSP
- LSP as dark matter: requires LSP to be neutral and uncolored
 - escapes from detector → missing energy

Mass spectrum [controlled by SUSY breaking and RGEs]

- Heavier particles decay through a cascade of lighter particles
 - High multiplicity of objects in SUSY events – multijets, multileptons
- NLSP affects event content:
 - light stau → events with taus
 - light sbottom → events with b -jets

Couplings

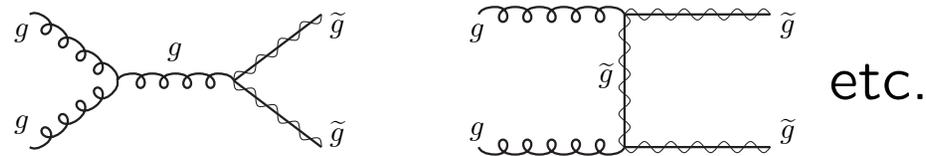
- In general, couplings are just the supersymmetrized version of SM couplings. Necessary to preserve solution to the hierarchy problem!

Superparticle production at hadron colliders

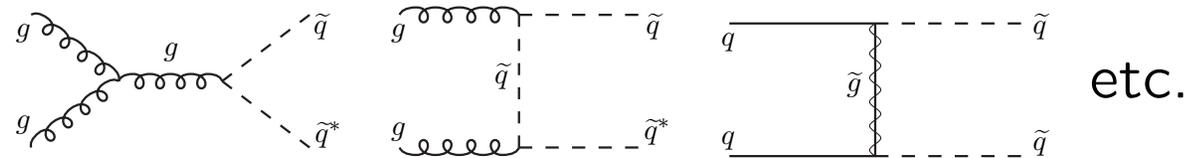
SUSY particles are produced in pairs (because of R-parity).

Production via QCD generally dominates, even though squarks and gluinos are typically heavy:

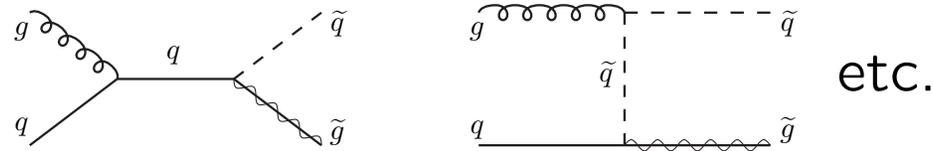
Gluino pairs



Squark pairs



Squark + gluino

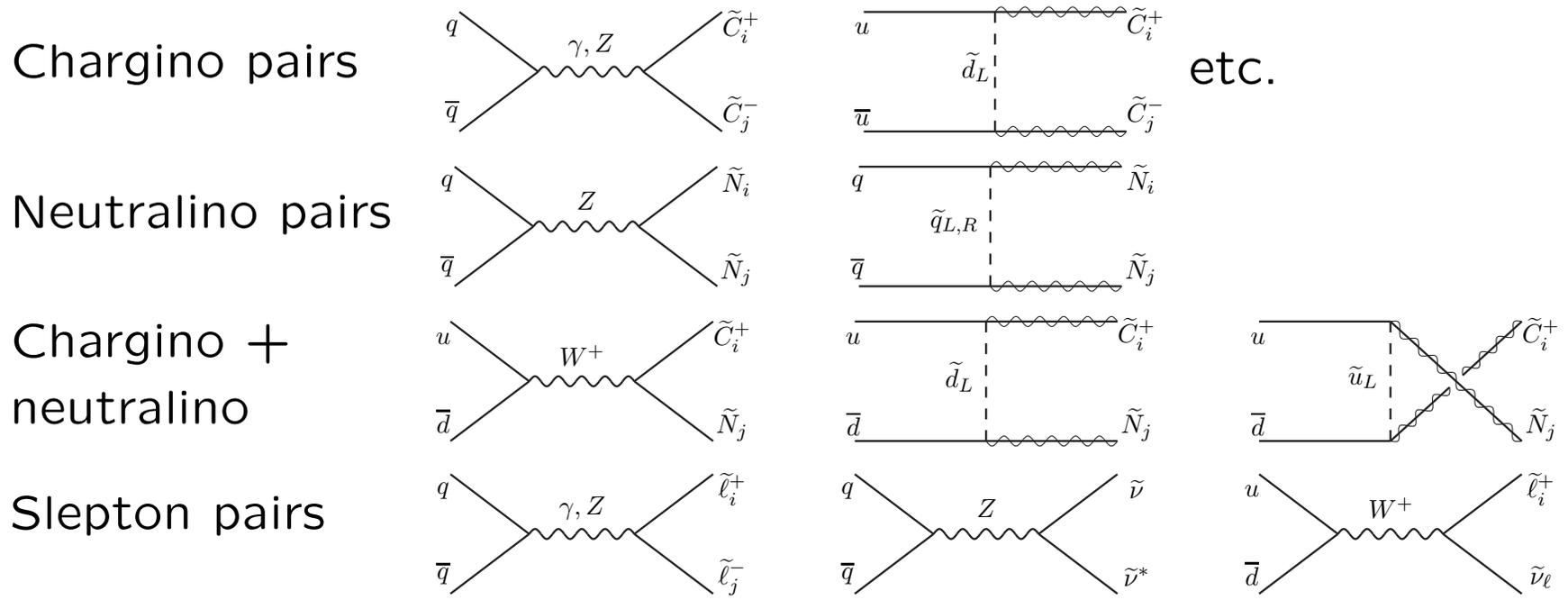


LHC reach depends on mass spectrum.

Reach for gluinos & squarks is typically out to about 2 TeV.

Superparticle production at hadron colliders

Production via electroweak interactions is also possible.



Rates are smaller than for colored particles because production cross sections involve EW couplings.

Superparticle decays

Glينو decays: always to $q \tilde{q}$.

If $M_{\tilde{g}} < M_{\tilde{q}}$, then gluino will decay via an off-shell squark:

3-body decays, $\tilde{g} \rightarrow q \tilde{q}^* \rightarrow q \bar{q} \tilde{N}_i$ or $q \bar{q}' \tilde{C}_i$

Squark decays:

To $q \tilde{g}$ (strong coupling) if kinematically allowed.

Otherwise $q \tilde{N}$ or $q \tilde{C}$ or (for 3rd gen.) $q \tilde{H}$.

Decay branching fractions controlled by squark and -ino compositions.

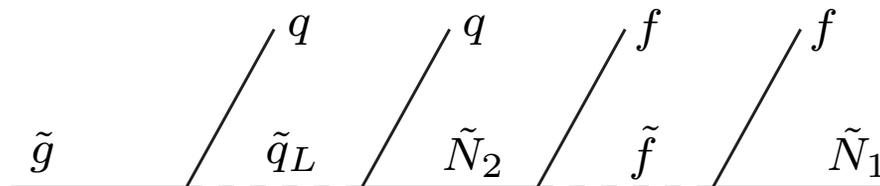
Slepton decays: to $\ell \tilde{N}$ or $\ell \tilde{C}$ ($\ell = \ell^\pm$ or ν as appropriate)

Neutralino and chargino decays: to $\ell \tilde{\ell}$ or $q \tilde{q}$,

or to gauge or Higgs boson + lighter neutral-/charg-ino

Typically get **decay chains**, which always end with the LSP.

For example:



Generic signatures of SUSY at hadron colliders:

Missing transverse energy

- From two escaping LSPs

Large jet multiplicity

- Produce heavier SUSY particles via QCD; long decay chains

Large $\sum E_T$ in event

- Decay of heavy particles produces energetic jets, leptons
- Relatively spherical distribution in detector

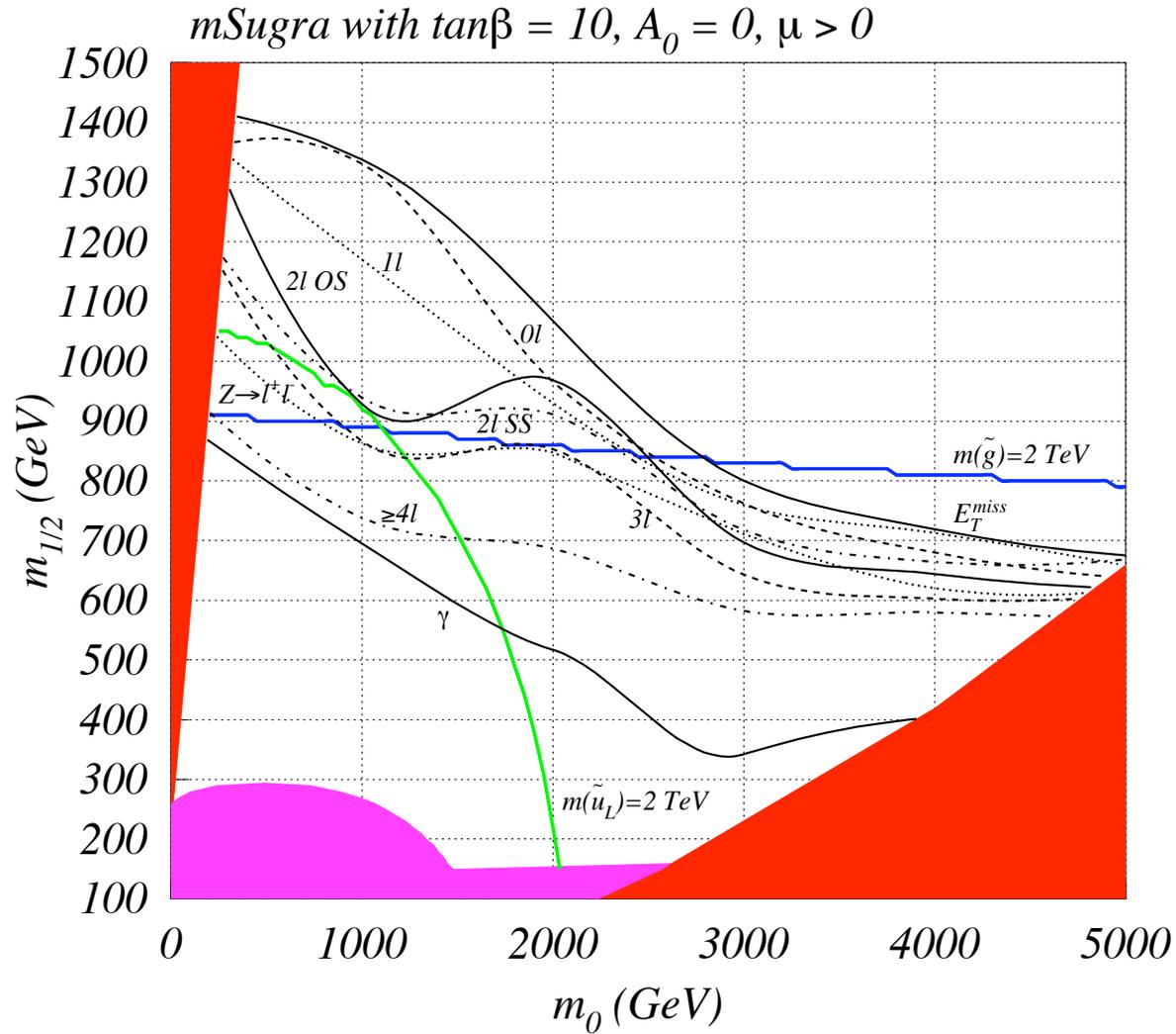
Like-sign leptons or b -jets

- Gluino is Majorana—decays equally likely to $q\tilde{q}^*$ or $\bar{q}\tilde{q}$
- Decay chain gives leptons—like-sign if $qq\tilde{q}^*\tilde{q}^*$ or $\bar{q}\bar{q}\tilde{q}\tilde{q}$

Many more specific signatures have been studied in detail.

Signatures depend strongly on mass spectrum.

LHC reach for discovering SUSY [an example in mSUGRA]



from Baer, Balázs, Belyaev, Krupovnickas, & Tata, hep-ph/0304303

SUSY breaking and phenomenological problems

The flavor sector has features that happen “by accident” in the Standard Model that must be engineered in the MSSM.

Small flavor-changing neutral currents

- SM: GIM mechanism
- MSSM: generic set of SUSY-breaking squark and slepton mass terms cause large mixing: disastrously huge contributions to flavor-changing observables.

CP violation appears to come only from phase of the CKM matrix

- SM: CKM matrix is the only possible source of CP violation (aside from $\theta_{\text{QCD}}\dots$)
- MSSM: generic set of SUSY-breaking couplings can have lots of new CP-violating phases: disastrously huge contributions to CP-violating observables (electric dipole moments, etc.)

Solutions to these problems drive the form of the SUSY-breaking mediation mechanisms.

SUSY-breaking models try to keep SUSY breaking “**flavor-blind**”, so that the only flavor dependence comes from the CKM matrix.

- Prevents large flavor-changing effects that would come from different mixing among squarks than among quarks
- Prevents large CP-violation by avoiding new phases in squark sector

Make the 3 generations of each squark type degenerate at the high scale:

- characteristic mass patterns in low-energy spectrum due to RGE running
- squark flavors correspond to quark flavors

SUSY-breaking mediation mechanisms

“Minimal supergravity” (mSUGRA), also called the Constrained MSSM (CMSSM)

- Non-universal scalar mass model (for dark matter)

Gauge-mediated SUSY breaking (GMSB)

Anomaly-mediated SUSY breaking (AMSB)

“Minimal supergravity” (mSUGRA)

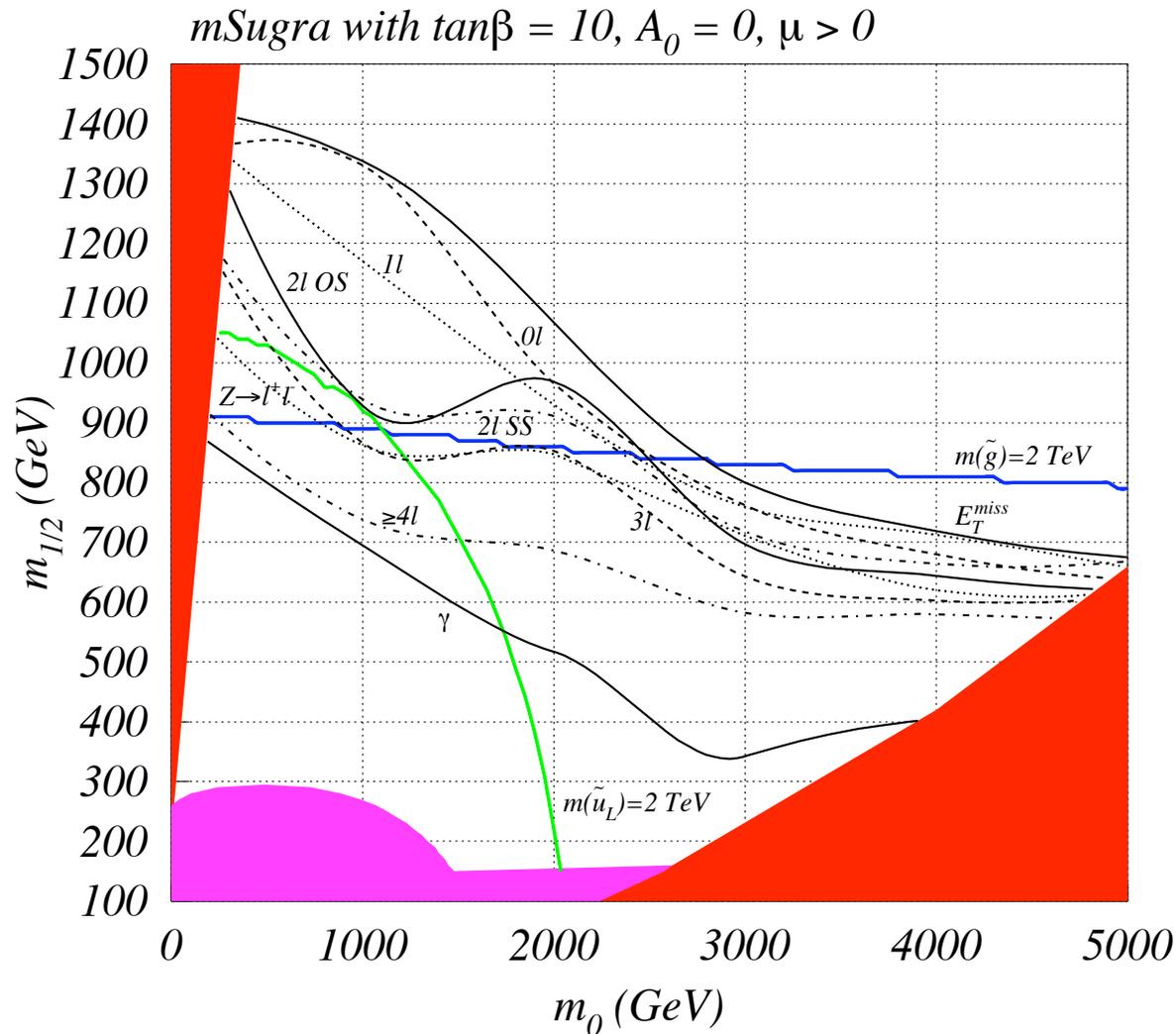
Rationale:

- Any SUSY-breaking hidden sector is bound to interact with visible sector via gravity.
- Gravity doesn't care about any particle properties (other than mass), except maybe spin.

“Four and a half” free parameters:

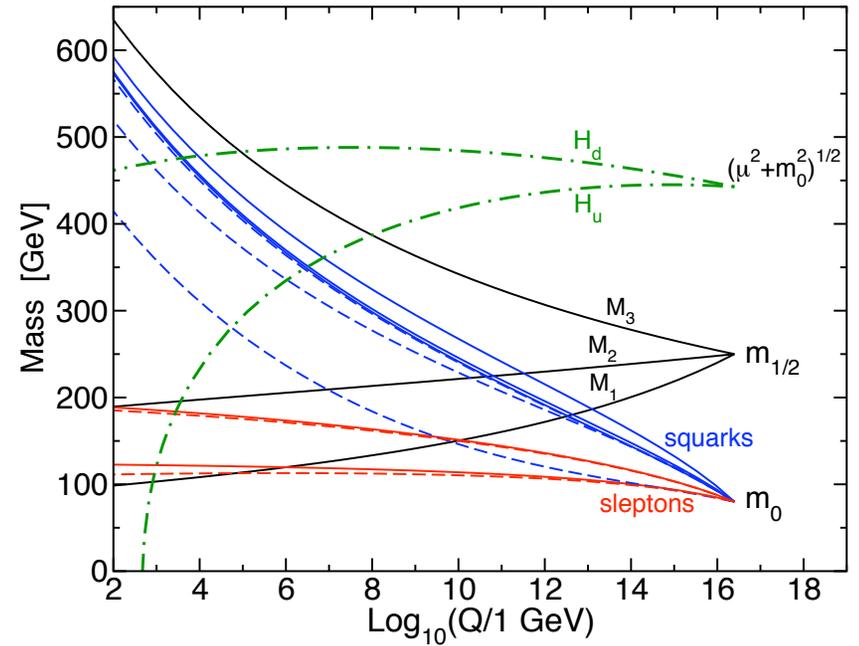
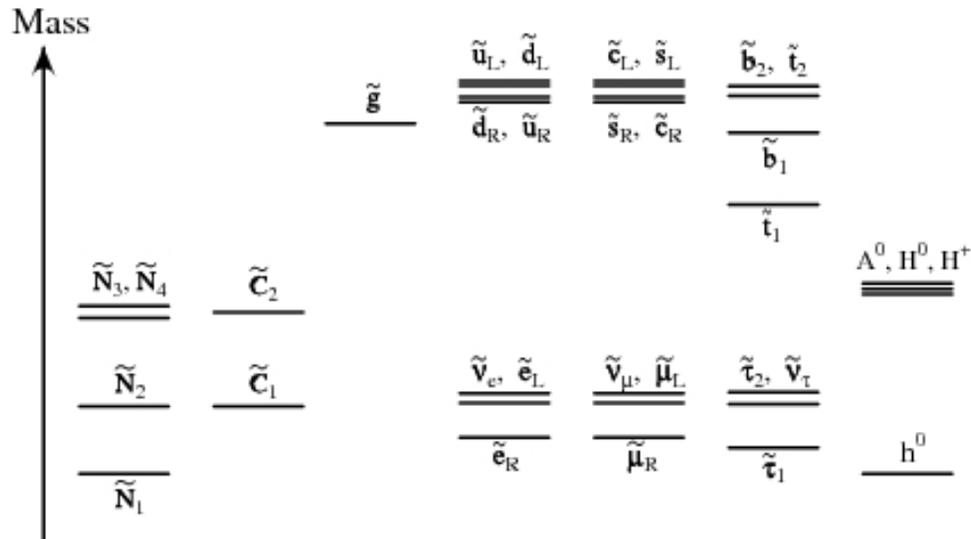
- Common scalar mass m_0
- Common gaugino mass $m_{1/2}$
- $\tan \beta$ (trade for, e.g., b after minimizing the Higgs potential)
- A squark/slepton trilinear coupling called A_0
- The sign of μ (SUSY-preserving parameter)—magnitude of μ is fixed by getting the right W mass from EWSB

Can plot things in a nice low-dimensional parameter space in terms of the high-scale parameters:



from Baer, Balázs, Belyaev, Krupovnickas, & Tata, hep-ph/0304303

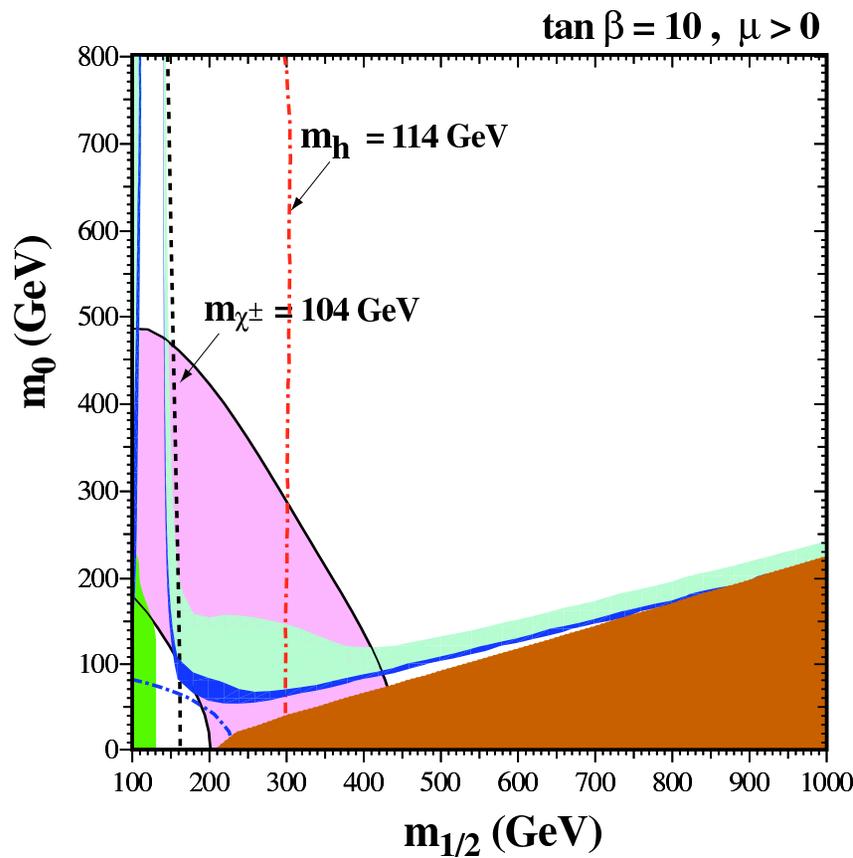
Complicated-looking spectrum, but mostly controlled by RGEs.



from Martin, hep-ph/9709356

mSUGRA with non-universal scalar masses (NUHM)

In mSUGRA, regions with acceptable dark matter density look very fine-tuned. (Hard to get enough annihilation)



“Bulk region”:

- \tilde{N}_1 mostly bino
- Light superparticles: mostly ruled out

“Stau coannihilation”:

- Large $m_{1/2}$
- $\tilde{\tau}_1$ only slightly heavier than \tilde{N}_1

“Focus point”:

- Large m_0 ; μ becomes small
- \tilde{N}_1 is mixed bino-Higgsino

Can relax fine-tuning if m_0 for the Higgses is different from m_0 for the squarks/sleptons.

Motivated by SO(10) SUSY GUT:

- Higgs multiplets live in one SO(10) representation while SM fermions all live in a different one.
- “Natural” to have a different m_0 parameter for the different SO(10) multiplets.
- Gauge groups are unified \rightarrow should have common gaugino mass at high scale.

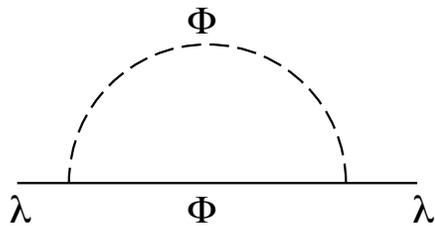
Make Higgsinos lighter; get mixed bino-Higgsino LSP without as much fine-tuning.

Gauge-mediated SUSY breaking (GMSB)

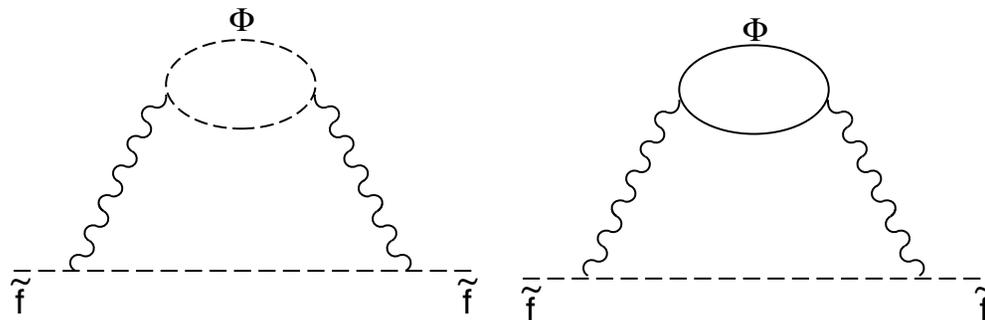
Mechanism:

- SUSY breaking happens in a field in the “hidden sector”
- That field couples to some chiral supermultiplets (the “messengers”), giving them mass M_{mess} and splitting the scalar/fermion masses by the SUSY breaking scale-squared F_{SUSY}
- The messengers are **charged under SM gauge group(s)**—SUSY breaking is induced in the visible sector by loops involving gauge interactions.

Gaugino masses:



Sfermion masses:



Figures from Giudice & Rattazzi, Phys. Rept. 322, 419 (1999), GMSB review article

Nice features of GMSB:

- Very predictive: only 2 SUSY-breaking parameters F_{SUSY} and M_{mess} ; otherwise depends only on number of messengers and their gauge charges.
- Gauge couplings are flavor-blind: avoid FCNC problems!
- Less ad-hoc than mSUGRA; does not involve nonrenormalizable supergravity.
- Mass scale of SUSY-breaking physics can be much lower.

$$M_{\text{SUSY}} \sim \text{TeV} \simeq C_{\text{mess}} \frac{F_{\text{SUSY}}}{M_{\text{mess}}} \quad (C_{\text{mess}}: \text{coefficient from messenger couplings})$$

Interesting new phenomenology:

- Fermionic part of the field that causes SUSY-breaking (“goldstino”) gets eaten by gravitino, giving it mass.
- Gravitino mass is $M_{\tilde{G}} \sim \frac{F_{\text{SUSY}}}{M_{\text{Pl}}} \sim \frac{1}{C_{\text{mess}}} \frac{\text{TeV} \times M_{\text{mess}}}{M_{\text{Pl}}}$
- For low M_{mess} , F_{SUSY} can be small: gravitino can be the LSP!

Next-lightest SUSY particle (NLSP) decays into gravitino, plus another particle depending on NLSP's identity.

Gravitino (really goldstino) couplings can be very weak: NLSP can have macroscopic decay length.

Photino NLSP: $\tilde{N}_1 \rightarrow \tilde{G}\gamma$

SUSY events all contain two hard photons.

Macroscopic decay length means displaced vertices, non-pointing photons.

Slepton NLSP: metastable heavy charged particle.

Slow minimum-ionizing tracks, displaced charged-lepton vertices.

Decays in the cavern wall if lifetime long enough.

Gravitino dark matter:

Terrible implications for direct or indirect detection because DM particle is super-weakly interacting.

Anomaly-mediated SUSY breaking (AMSB)

Special case of gravity mediation:

- No tree-level coupling to communicate SUSY breaking to visible sector.
- SUSY-breaking mediated by loop effects (also present in mSUGRA, but much smaller than tree-level).
- Flavor-blind. [Simplest models have negative slepton mass-squared: have to introduce scalar mass parameter m_0^2 to fix it up.]

Gaugino masses generated at one-loop by the “superconformal anomaly” from the gravitino mass:

$$M_a = b_a^{\text{MSSM}} \left(\frac{\alpha_a}{4\pi} \right) m_{3/2}$$

$b_a^{\text{MSSM}} = \left(\frac{33}{5}, 1, -3 \right)$ are the gauge beta functions

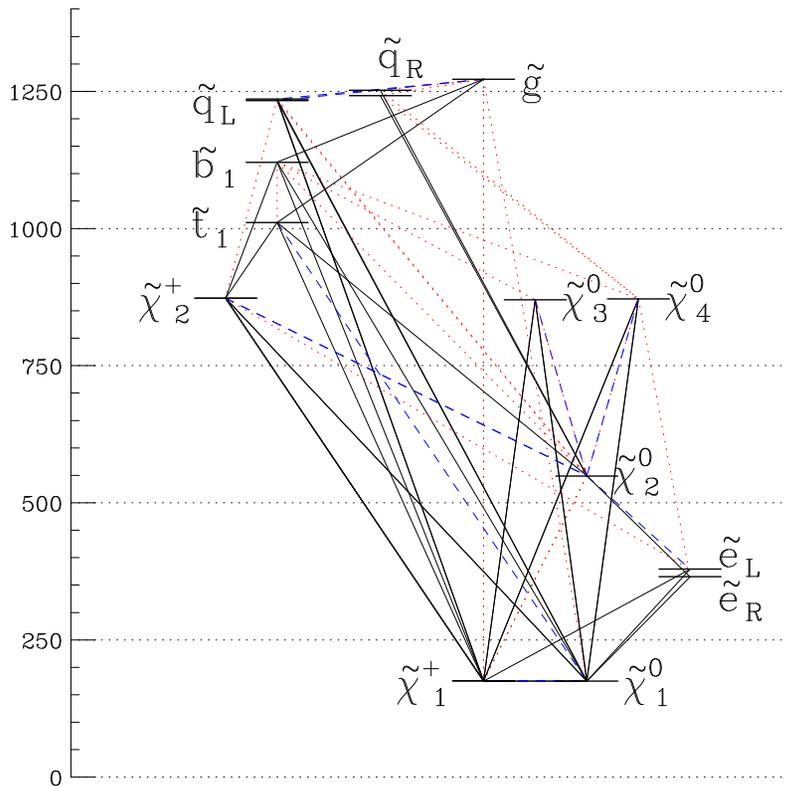
Minus signs in fermion masses can be eliminated by field redefinition—not physical.

After RGE running, $M_1 : M_2 : M_3 = 2.8 : 1 : 8.3$.

Wino is lightest!

Dramatic impact on phenomenology:

- \tilde{N}_1 and \tilde{C}_1^\pm are nearly degenerate: typically $\Delta M \lesssim \text{GeV}$.
- \tilde{C}_1^\pm decays almost exclusively into \tilde{N}_1 plus a soft π^\pm .
- \tilde{C}_1^\pm can have detectably-long decay length.



Benchmark point SPS9

Can have other patterns for sfermion mass scale.

Key feature is the nearly-degenerate lightest neutralino & chargino.

Still see missing E_T .

Barr et al, JHEP 0303, 045 (2003)

Maybe it's something else entirely?

“SUSY without prejudice” :

Berger et al, JHEP 0902, 023 (2009)

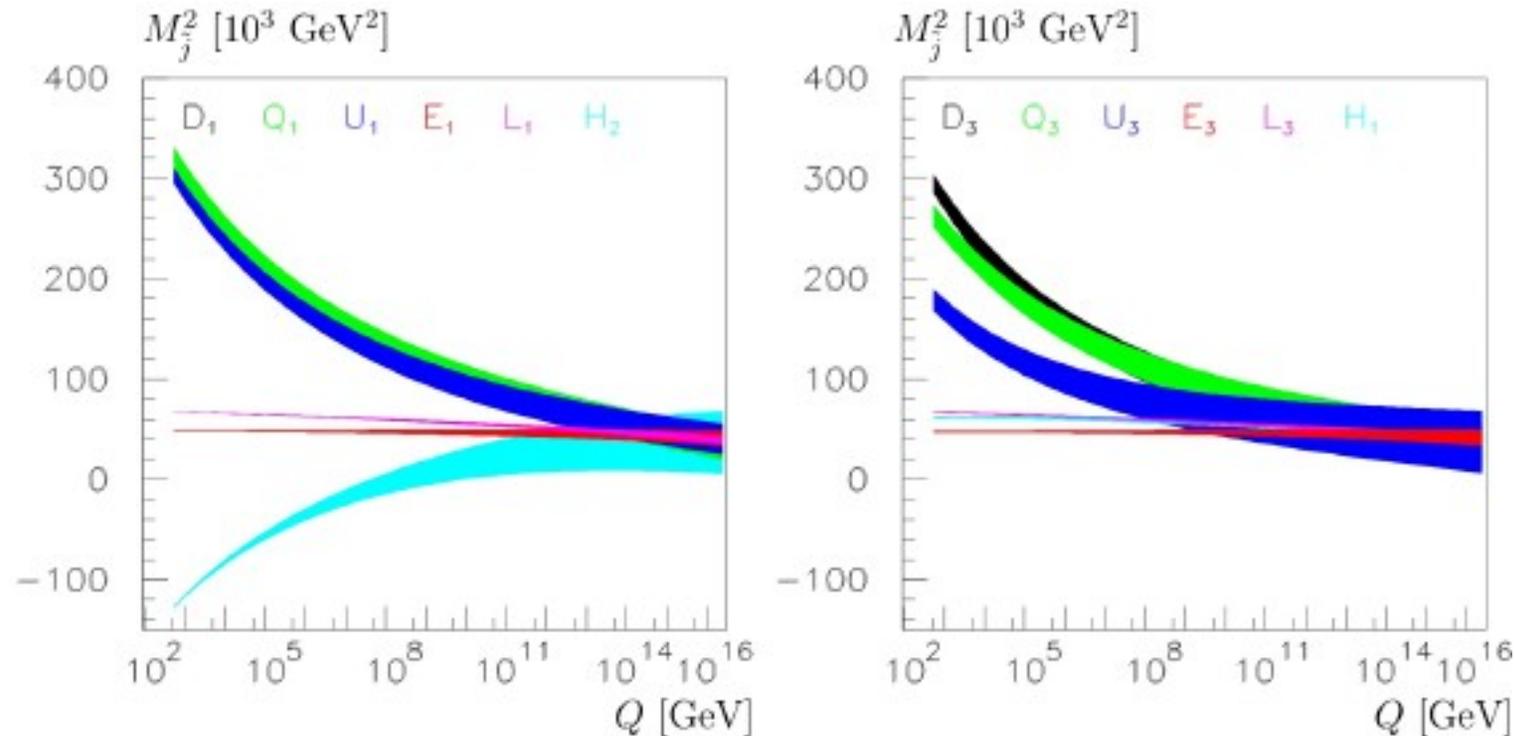
- Randomly sample a general CP-conserving MSSM with minimal flavor violation
- Impose all expt constraints and DM requirement (upper bound)
- Generate signal MC and survey characteristic signatures

Much broader set of predictions for SUSY properties, expt observables than in standard benchmarks.

Reconstructing the high-scale theory

The RGEs will let us extrapolate the high-scale physics based on measurements of the EW scale parameters.

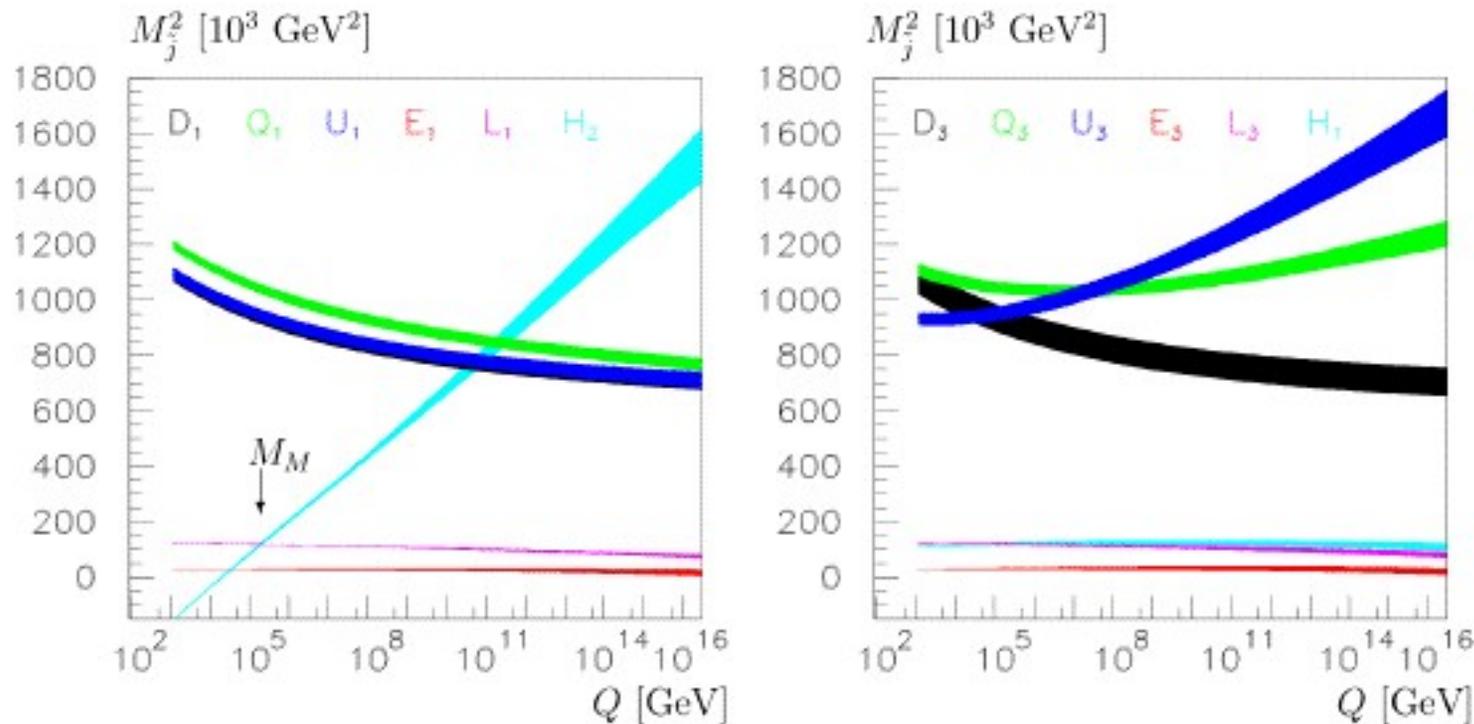
Sample mSUGRA spectrum:



from Blair, Porod & Zerwas, [hep-ph/0210058](https://arxiv.org/abs/hep-ph/0210058)

Run soft-SUSY-breaking parameters up, see if they unify:
insight into physics at the highest energy scale!

Contrast gauge-mediated SUSY breaking spectrum:



from Blair, Porod & Zerwas, hep-ph/0210058

Soft-SUSY-breaking parameters do not unify in GMSB:
they are related to beta-functions at the messenger scale M_{mess} .

This is the real motivation for measuring SUSY masses and couplings. Need high precision as much as possible.

Measure SUSY masses and couplings

A new challenge:

- Each SUSY event contains *two* invisible massive particles.
- Can't reconstruct invariant mass bumps.
- Can't even measure transverse mass like for $W \rightarrow l\nu$.

Need to use more sophisticated techniques:

Take advantage of decay chains.

- Kinematic endpoints
- Four-momentum conservation relations
- Other kinematic tricks

(More on this in Lecture 4.)

Summary

SUSY discovery prospects generically good at LHC

- Lots of jets, missing p_T

SUSY phenomenology is mostly controlled by the mass spectrum.

- SUSY-breaking mediation mechanism
- Renormalization-group running

Potential insight into the highest energy scales through the pattern of SUSY-breaking masses

Near-term challenge:

- Discover new physics!
- See whether it's SUSY by measuring couplings, spins
- Measure masses, other coups and reconstruct high-scale theory